

## Ion Dependent Computation for Electronic Dielectric Constants of Mixed Crystals in Rocksalt and Zinc blende Structures

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### Abstract

Quantum ion dependent theory for electronic dielectric constants of  $A^N B^{8-N}$  binary solids has been extended to the II-VI crystals mixed in different proportions. The values of optical dielectric constants ( $\epsilon_\infty$ ) are evaluated for a number of mixed crystals, which are found to agree with available experimental values. The results agree well with the predictions from well established Clausius-Mossotti relation also. Thus, it gives a strong support to the validity of ion dependent formulation for mixed crystals.

**Key words:** Electronic Dielectric Constant ( $\epsilon_\infty$ ), Interionic Separation (R), Mixed Crystals

### Introduction

The electronic dielectric behaviour of binary crystals remained a topic of great interest in last few decades as it is a subject of great experimental importance in electronic industry. The varied values of optical dielectric constants ( $\epsilon_\infty$ ) and average energy gaps ( $E_g$ ) of ionic and covalent crystals have helped in developing many components for photo elastic, photo conducting and solar cell devices. For the study of dielectric behaviour, a number of classical models have been prescribed. However, the average energy gap is a quantum concept, hence a good number of quantum theories are also prescribed. Most satisfactory results are obtained through the quantum ion dependent model<sup>(1 to 5)</sup> established in last two decades. The model says that the dielectric behaviour of ionic crystals and partial ionic-covalent solids (with dominating ionic contribution) is completely cation dependent. The relation between  $\epsilon_\infty$  and the interionic separation R is suggested as<sup>(1)</sup>

$$\epsilon_\infty = 1 + BR^S \quad (1)$$

where B is a characteristic constant of a particular cation and S is a family characteristic constant. This ion dependent model is well appreciated in the review article of Moss<sup>(6)</sup>.

In the present paper we propose to mix the solids of rocksalt and zinc blende structures, specially in partial ionic-covalent family II-VI. Mixed solids in different proportions are taken up and their electronic dielectric constants are evaluated by using the ion dependent concept.

### Theory and Method of Calculation

Any two crystals X and Y with same cation in binary II-VI family are mixed in different proportion  $\lambda_x$  and  $\lambda_y$  respectively. The interionic separation of the mixed crystal (R) is found through the relation

$$R^3 = \lambda_x R_x^3 + \lambda_y R_y^3 \quad (2)$$

where  $R_x$  and  $R_y$  are the interionic separations of the pure II-VI crystals X and Y respectively. This formula is in accordance with the concept of volume mixing<sup>(7,8)</sup>. Calculated values of R for mixed crystals in different proportions are reported in tables 1 to 6. Since we are mixing two same cation solids, values of characteristic constants B and S for same cations are directly taken up from the tables, earlier predicted for pure II-VI family through ion dependent formulation<sup>(1)</sup>. Thus, by using the values of R obtained from eqn. (2), we predict the values of  $\epsilon_\infty$  for different mixed crystals through eqn. (1). Tables 1 to 6 show the calculated values of  $\epsilon_\infty$  through ion dependent calculations.

In order to check the validity of the results we call back the well established classical Clausius Mossotti relation for electronic dielectric constants

$$\frac{\epsilon_{\infty} - 1}{\epsilon_{\infty} + 2} = \frac{4\pi}{3} \frac{\alpha}{V} \quad (3)$$

where  $\alpha$  and  $V$  are the polarisability and volume per ion pair of the crystal respectively.

Kamiyoshi and Niagra<sup>(9)</sup> and Varotsos<sup>(10)</sup> considered the polarisability of mixed crystal to be equal to the sum of polarisabilities of the pure crystals taken in the proportion of mixing ratio. Thus eqn. (3) in modified<sup>(11)</sup> as

$$\frac{\epsilon_{\infty} - 1}{\epsilon_{\infty} + 2} = \lambda_x \left[ \frac{(\epsilon_{\infty})_x - 1}{(\epsilon_{\infty})_x + 2} \right] + \lambda_y \left[ \frac{(\epsilon_{\infty})_y - 1}{(\epsilon_{\infty})_y + 2} \right] \quad (4)$$

using experimental values of  $(\epsilon_{\infty})_x$  and  $(\epsilon_{\infty})_y$  for pure II-VI crystals<sup>(1)</sup>,  $\epsilon_{\infty}$  for mixed crystals are evaluated from eqn (4). These values are also reported in table 1 to 6 for comparison.

**Table – 1 : Rocksalt Structure**

MgS – MgSe (% MgSe)	R	$(\epsilon_{\infty})_a$	$(\epsilon_{\infty})_b$	$(\epsilon_{\infty})_{Exp.}$
0	2.60	5.09	5.09	<b>5.1</b>
10	2.61	5.16	5.16	-
20	2.63	5.22	5.25	-
30	2.64	5.29	5.32	-
40	2.65	5.35	5.38	-
50	2.67	5.42	5.46	-
60	2.68	5.48	5.56	-
70	2.69	5.54	5.63	-
80	2.70	5.61	5.71	-
90	2.72	5.67	5.79	-
100	<b>2.73</b>	<b>5.74</b>	<b>5.89</b>	<b>5.9</b>

**Table – 2 : Rocksalt Structure**

CaO – CaS (%CaS)	R	$(\epsilon_{\infty})_a$	$(\epsilon_{\infty})_b$	$(\epsilon_{\infty})_{Exp.}$
0	2.40	3.21	3.30	<b>3.3</b>
10	2.45	3.36	3.40	-
20	2.50	3.50	3.50	-
30	2.55	3.65	3.61	-
40	2.59	3.79	3.71	-
50	2.64	3.94	3.84	-

60	2.68	4.08	3.96	-
70	2.72	4.23	4.08	-
80	2.76	4.37	4.21	-
90	2.80	4.52	4.35	-
100	<b>2.84</b>	<b>4.66</b>	<b>4.49</b>	<b>4.5</b>

**Table – 3 : Rocksalt Structure**

SrSe – SrTe (% SrTe)	R	$(\epsilon_{\infty})_a$	$(\epsilon_{\infty})_b$	$(\epsilon_{\infty})_{Exp.}$
0	3.12	5.04	4.90	<b>4.9</b>
10	3.13	5.09	4.98	-
20	3.14	5.14	5.06	-
30	3.16	5.18	5.14	-
40	3.17	5.23	5.23	-
50	3.18	5.28	5.32	-
60	3.19	5.33	5.41	-
70	3.20	5.38	5.50	-
80	3.22	5.42	5.59	-
90	3.23	5.47	5.69	-
100	<b>3.24</b>	<b>5.52</b>	<b>5.79</b>	<b>5.8</b>

**Table – 4 : Zinc blende Structure**

BeS – MeSe (% BeSe)	R	$(\epsilon_{\infty})_a$	$(\epsilon_{\infty})_b$	$(\epsilon_{\infty})_{Exp.}$
0	2.10	6.48	7.09	<b>7.1</b>
10	2.11	6.56	7.11	-
20	2.12	6.65	7.13	-
30	2.13	6.73	7.15	-
40	2.14	6.81	7.17	-
50	2.15	6.89	7.19	-
60	2.16	6.97	7.21	-
70	2.17	7.06	7.23	-
80	2.18	7.14	7.25	-
90	2.19	7.22	7.27	-
100	<b>2.20</b>	<b>7.30</b>	<b>7.29</b>	<b>7.3</b>

**Table – 5 : Zinc blende Structure**

ZnS – ZnSe (% ZnSe)	R	$(\epsilon_{\infty})_a$	$(\epsilon_{\infty})_b$	$(\epsilon_{\infty})_{Exp.}$
0	2.36	5.38	5.19	<b>5.2</b>
10	2.37	5.43	5.26	-
20	2.38	5.48	5.32	-
30	2.39	5.53	5.39	-
40	2.40	5.58	5.46	-
50	2.40	5.64	5.53	-
60	2.41	5.69	5.60	-

<b>70</b>	2.42	5.74	5.67	-
<b>80</b>	2.43	5.79	5.74	-
<b>90</b>	2.44	5.85	5.82	-
<b>100</b>	<b>2.45</b>	<b>5.90</b>	<b>5.89</b>	<b>5.9</b>

$$\epsilon_{\infty} = n^2 \quad (5)$$

Thus one can derive proper crystal mixture for any definitely required refractivity in opto-electronic systems.

**Table – 6 : Zinc blende Structure**

CdS – CdTe (% CdTe)	R	( $\epsilon_{\infty}$ ) <sub>a</sub>	( $\epsilon_{\infty}$ ) <sub>b</sub>	( $\epsilon_{\infty}$ ) <sub>Exp.</sub>
<b>0</b>	2.52	5.53	5.19	<b>5.2</b>
<b>10</b>	2.55	5.68	5.35	-
<b>20</b>	2.58	5.84	5.52	-
<b>30</b>	2.60	5.99	5.70	-
<b>40</b>	2.63	6.15	5.88	-
<b>50</b>	2.66	6.30	6.07	-
<b>60</b>	2.68	6.46	6.28	-
<b>70</b>	2.71	6.61	6.49	-
<b>80</b>	2.73	6.77	6.72	-
<b>90</b>	2.75	6.92	6.95	-
<b>100</b>	<b>2.78</b>	<b>7.08</b>	<b>7.20</b>	<b>7.2</b>

**Analysis of Results**

A comparison of ( $\epsilon_{\infty}$ )<sub>a</sub> evaluated from quantum ion dependent formulation and ( $\epsilon_{\infty}$ )<sub>b</sub> predicted from classical Clausius Mossotti relation in tables 1 to 6 shows excellent agreement. Close matching of the results from two entirely different approaches proves the reliability of the values of electronic dielectric constants of mixed crystals in II-VI binary family. Thus quantum ion dependent formulation can be used to predict the electronic dielectric constant of the mixed crystals in ionic I-VII solids as well as covalent III-V semiconductors also, since the basic cation anion dependent theory covers all subsets of binary A<sup>N</sup> B<sup>8-N</sup> family<sup>(1)</sup>.

Other kinds of quantum approaches for the developments in the theory of mixed crystals have been considered, but only for pure ionic crystals<sup>(12)</sup>. Covalent semiconductors have not been touched at all till to date. The present approach through quantum ion dependent formulation can be well applied for covalent semiconductors also. In a wider arena, a huge range of values of  $\epsilon_{\infty}$  can be obtained by mixing the crystals in different proportions, which can be used for many different purposes. The electronic dielectric constant has a direct bearing on the optical refractive index (n) as

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